

ΘΕΜΑ Α

Α ΓΙΑΝΤΗΣΕΚ (ΠΑΛΑΙΟ ΣΥΣΤΗΜΑ)

A<sub>1</sub>) β , A<sub>2</sub>) γ , A<sub>3</sub>) α A<sub>4</sub>) α

A<sub>5</sub>) Σ , Λ , Λ , Λ , Σ

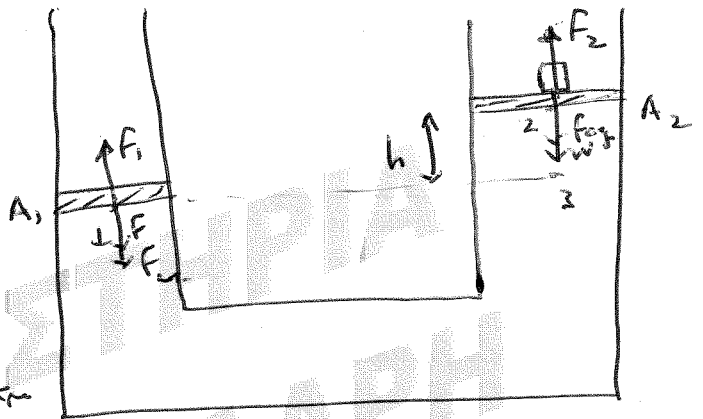
B<sub>1</sub>) 16x021 P<sub>1</sub>=P<sub>3</sub> ⇔

$$P_1 = P_2 + \rho gh \quad (1)$$

Eq<sub>1</sub>:  $\Sigma F = 0 \Rightarrow F_1 = F + F_{atm}$

$$P_1 = \frac{F}{A_1} + P_{atm} \quad (2)$$

Eq<sub>2</sub>:  $\Sigma F = 0 \Rightarrow F_2 = F_{atm} + W \Rightarrow P_2 = P_{atm} + \frac{W}{A_2} \quad (3)$



(1)  $\stackrel{(2)}{\Rightarrow}$   $\frac{F}{A_1} + P_{atm} = P_{atm} + \frac{W}{A_2} + \rho gh \quad \Leftarrow$

$$\Rightarrow \frac{F}{A_1} = \frac{W + \rho gh A_2}{A_2}$$

Σωστό το (ii)

B2)

$x_1$   $\Sigma \omega_1 \times \omega_2 \text{ cm}$

$x_2 = x_1 + 4 \text{ cm}$   $\alpha \eta \sigma \beta \Sigma \text{ cm}$

$$r_B - r_A = N\lambda \quad (1)$$

$$r_B' - r_A = (2N+1)\frac{\lambda}{2} \quad (2)$$

$$(2) - (1) \quad r_B' - \cancel{r_A} - r_B + \cancel{r_A} = (2N+1)\frac{\lambda}{2} - N\lambda$$

$$(r_B + 2\Delta x) - r_B = N\lambda + \frac{\lambda}{2} - N\lambda \Rightarrow 2(x_2 - x_1) = \frac{\lambda}{2} \Rightarrow$$

$$\Rightarrow 2 \cdot 4 = \frac{\lambda}{2} \Rightarrow \boxed{\lambda = 16 \text{ cm}}$$

$\Sigma \omega_1 \times \omega_2$   $\text{TO } \underline{\underline{ii}}$

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B3 iii

Πρώτη κρούση:  $U_1' = \frac{m_1 - m_2}{m_1 + m_2} U_1$ ,  $U_2' = \frac{2m_1 U_1}{m_1 + m_2}$

$$\Pi_1 \% = \frac{\Delta K_2}{K_{\text{αρχ}}} \cdot 100\% = \frac{\frac{1}{2} m_2 U_2'^2}{\frac{1}{2} m_1 U_1^2} \cdot 100\% = \frac{m_2 \frac{4m_1^2 U_1^2}{(m_1 + m_2)^2}}{m_1 U_1^2} \cdot 100\%$$

$$\Pi_1 \% = \frac{4m_1 m_2}{(m_1 + m_2)^2} \cdot 100\%$$

Δεύτερη κρούση:  $U_2' = \frac{m_2 - m_1}{m_1 + m_2} U_2$ ,  $U_1' = \frac{2m_2 U_2}{m_1 + m_2}$

$$\Pi_2 \% = \frac{\Delta K_1}{K_{\text{αρχ}}} \cdot 100\% = \frac{\frac{1}{2} m_1 U_1'^2}{\frac{1}{2} m_2 U_2^2} \cdot 100\% = \frac{m_1 \frac{4m_2^2}{(m_1 + m_2)^2} \cdot U_2^2}{m_2 U_2^2} \cdot 100\%$$

$$\Pi_2 \% = \frac{4m_1 m_2}{(m_1 + m_2)^2} \cdot 100\%$$

$$\frac{\Pi_1}{\Pi_2} = \frac{\frac{4m_1 m_2}{(m_1 + m_2)^2} \cdot 100\%}{\frac{4m_1 m_2}{(m_1 + m_2)^2} \cdot 100\%} \Rightarrow \frac{\Pi_1}{\Pi_2} = 1 \Rightarrow \Pi_1 = \Pi_2 \quad \textcircled{ii}$$

ΘΕΜΑ Γ

- $m_1 = 1 \text{ kg}$
- $\theta = 30^\circ$
- $k = 100 \text{ N/m}$
- $h = 0,6 \text{ m}$
- $m_2 = 3 \text{ kg}$

- Γ1)  $v_{\text{κοιλι}}$
  - Γ2)  $A = ?$
  - Γ3)  $x(t)$
  - Γ4)  $k = 80$   
2η φάση
- $\frac{|F_{\text{ελ}}|}{|\Sigma F|} = ;$   
 $g = 10 \text{ m/s}^2$

Γ1) ΑΔΜΕ

⊙  $v = 0$

$$k_A + v_A = k_r + v_r$$

$$(v = 0) \rightarrow \odot \downarrow v_2$$

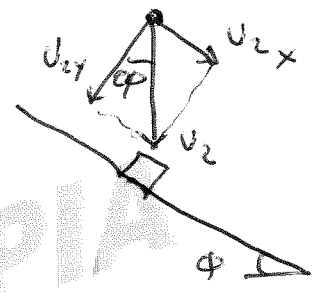
$$m_1 g h = \frac{1}{2} k v_2^2$$

$v_2 = 2\sqrt{3} \text{ m/s}$

ΑΔΟ (Αξόνως)

$$\vec{P}_2 + \vec{P}_1 = \vec{P}_{\Sigma} + \Sigma$$

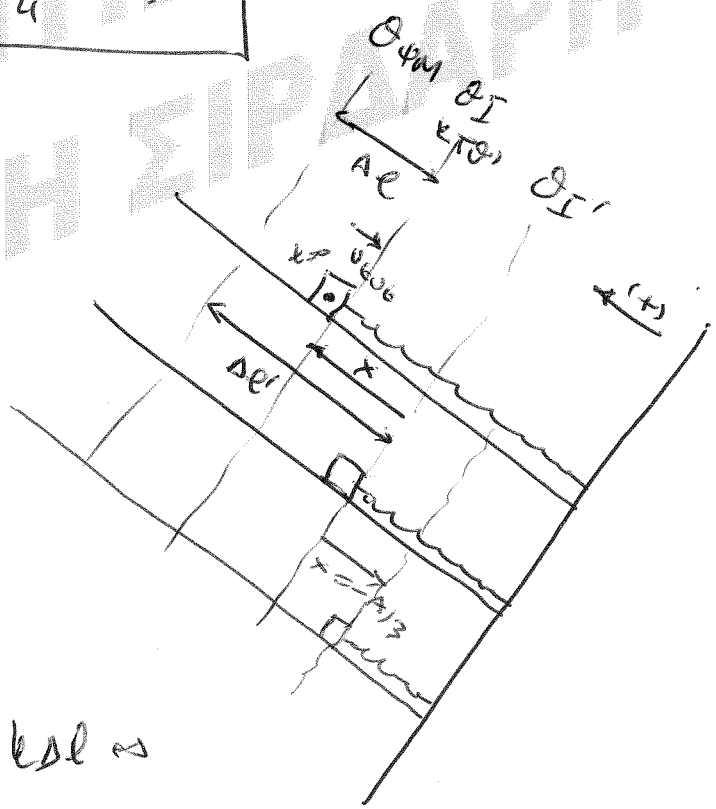
$$m_2 v_{2x} = (m_1 + m_2) v_{\text{κοιλι}}$$



$$m_2 v_2 \cdot \sin \phi = (m_1 + m_2) v_{\text{κοιλι}}$$

$v_{\text{κοιλι}} = \frac{3\sqrt{3}}{4} \text{ m/s}$

Γ2)



ΘΙ:  $\Sigma F = 0 \rightarrow$

$$m_1 x = F_{\text{ελ}} \Rightarrow m_1 g \sin \theta = k \Delta l \Rightarrow$$

$\Delta l = 0,05 \text{ m}$

ΘΙ':  $\Sigma F = 0 \Rightarrow (m_1 + m_2) g \sin \theta = k \Delta l' \Rightarrow$ 

$\Delta l' = 0,2 \text{ m}$

$$\text{Αρα } x = \Delta l' - \Delta l \Rightarrow \boxed{x = 0,15 \text{ m}}$$

$$E = K + U \Rightarrow \frac{1}{2} k A^2 = \frac{1}{2} (\omega_1 + \omega_2) v_0^2 + \frac{1}{2} k x^2 \Rightarrow$$

$$\Rightarrow \boxed{A = 0,3 \text{ m}}$$

$$(3) \quad k = (\omega_1 + \omega_2) \omega^2 \Rightarrow \omega = 5 \text{ rad/s}$$

$$I_{\text{CM}} = \frac{1}{2} m l^2 \quad t = 0, \quad x = 0,15 \text{ m} = \frac{A}{2}, \quad v < 0$$

$$x = A \sin(\omega t + \phi_0) \quad \left. \begin{array}{l} t=0 \\ x = \frac{A}{2} \end{array} \right\} \frac{A}{2} = A \sin \phi_0 \Rightarrow \sin \phi_0 = \frac{1}{2}$$

$$\phi_0 = 2k\pi + \frac{\pi}{6} \xrightarrow{v < 0} \phi_0 = \frac{\pi}{6} \quad \text{αναρ.}$$

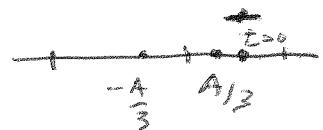
$$\phi_0 = 2k\pi + \frac{5\pi}{6} \xrightarrow{v < 0} \phi_0 = \frac{5\pi}{6} \quad \text{δεν υφίστ.$$

$$\text{Αρα } x = 0,3 \sin\left(5t + \frac{5\pi}{6}\right) \quad (\text{SI}).$$

$$(4) \quad k = 8U \Rightarrow E - U = 8U \Rightarrow E = 9U \Rightarrow$$

$$\frac{1}{2} k A^2 = 9 \cdot \frac{1}{2} k x^2 \Rightarrow x = \pm \frac{A}{3}$$

$$\begin{array}{l} 1^{\text{η}} \text{ φορά } x = A/3 \\ 2^{\text{η}} \text{ φορά } x = -A/3 \end{array}$$



$$\left| \frac{F_{E_1}}{\Sigma F} \right| = \frac{k(\Delta l' + A/3)}{|-k(-A/3)|} = \frac{0,3}{0,1} = 3.$$

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ΘΕΜΑ Δ

$M_1 = 6 \text{ kg}$

$m = 1 \text{ kg}$

$v = 0, 1 \text{ m}$

$L = 1 \text{ m}$

$R = 2, 8 \text{ m}$

$\eta = \phi = 0, 6$

$\beta = \alpha = 0, 8$

$\Delta 1) T = ;$

$M_2 = ;$

$\Delta 2) a_{\text{cm}} = ;$

$\Delta 3)$

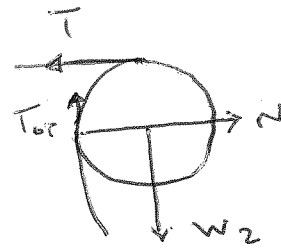
$\Delta 1) \text{ i) Δίκως}$

$\sum \tau_{(O)} = 0 \Rightarrow$

$T R - T_{OC} R = 0 \Rightarrow$

$T = T_{OC} \quad (1)$

$\sum F_y = 0 \Rightarrow W_2 = T_{OC} \Rightarrow W_2 = T \quad (2)$



Ραβδος

$\sum \tau_{(A)} = 0 \Rightarrow$

$\tau_{W_1} + \tau_w + \tau_T = 0 \Rightarrow$

$T \cdot \frac{l}{2} \sin \phi - W_1 \cdot \frac{l}{2} \cos \phi - W \cdot l \cos \phi = 0$

$T \cdot \frac{1}{2} \cdot 0,8 - 60 \cdot \frac{1}{2} \cdot 0,6 - 10 \cdot 0,6 = 0$

$\Rightarrow 0,4 T - 18 - 6 = 0 \Rightarrow \boxed{T = 60 \text{ N}}$

$\text{ii) } (2) \quad M_2 g = T \Rightarrow \boxed{M_2 = 6 \text{ kg}}$

$\Delta 2) \quad I_{OC} = I_p + I_{cm} = \frac{1}{3} M_1 L^2 + m L^2 \Rightarrow I_{OC} = 3 \text{ kg m}^2$

$\sum \tau = I_{OC} a_{\text{cm}} \Rightarrow m g \cdot l \cos \phi + M_1 g \cdot \frac{l}{2} \cos \phi = I_{OC} a_{\text{cm}} \Rightarrow$

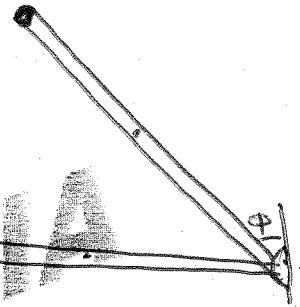
$$\Rightarrow 10 \cdot 0,6 + 60 \cdot \frac{0,6}{2} = 3 a_{\text{cm}} \Leftrightarrow$$

$$\Rightarrow 24 = 3 a_{\text{cm}} \Leftrightarrow a_{\text{cm}} = 8 \text{ rad/s}^2$$

$\Delta_3$ ) ΑΑΜΕ

$$\cancel{K_A + U_A} = \cancel{K_T} + \cancel{U_C}$$

$$m g \cdot l \sin \phi + M g \frac{l}{2} \sin \phi = \frac{1}{2} I \omega^2 \quad (U=0)$$



$$10 \cdot 0,8 + 60 \cdot 0,4 = \frac{1}{2} \cdot 3 \cdot \omega^2 \Rightarrow 8 + 24 = \frac{1}{2} \cdot 3 \omega^2 \Rightarrow$$

$$\omega = \frac{10}{\sqrt{3}} \Rightarrow \omega = \frac{8\sqrt{3}}{3} \text{ rad/s}$$

$$L_T = I \omega \Rightarrow L_T = 8\sqrt{3} \text{ kg m}^2/\text{s}$$

$$\Delta L = L_T - \cancel{L_{\text{app}}} \Rightarrow |\Delta L| = 8\sqrt{3} \text{ kg m}^2/\text{s}$$

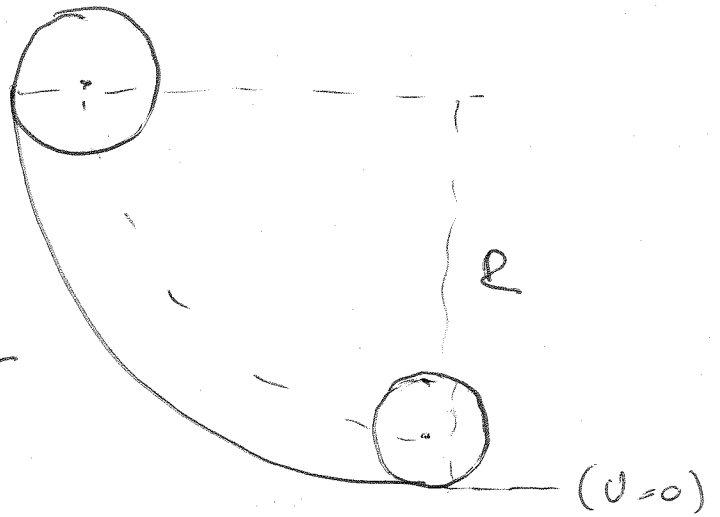
ii) φορα προς τα εξω ☺

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Δ4) ΑΔΜΕ

$\vec{v}_A + U_A = K_T + U_T$

$$M_2 g R = \frac{1}{2} I \omega^2 + \frac{1}{2} M_2 v_{cm}^2 + M_2 g r$$



$$M_2 g R = \frac{1}{2} \cdot \frac{1}{2} M_2 \cdot v_{cm}^2 \cdot \frac{v_{cm}^2}{R^2} + \frac{1}{2} M_2 v_{cm}^2 + M_2 g r$$

$$gR = \frac{1}{4} v_{cm}^2 + \frac{1}{2} v_{cm}^2 + g r \rightarrow g(R-r) = \frac{3}{4} v_{cm}^2$$

$$\Leftrightarrow v_{cm} = \sqrt{\frac{4g(R-r)}{3}} \rightarrow v_{cm} = \sqrt{\frac{4 \cdot 10 \cdot 27}{3}} \rightarrow \boxed{v_{cm} = 6 \text{ m/s}}$$

Δ5)

i)

$$N = \frac{S_{cm}}{2\pi r} = \frac{\frac{2\pi(R-r)}{4}}{2\pi r} = \frac{R-r}{4r} = \frac{27}{0,4 \cdot 4} = \underline{\underline{27 \text{ nsp}}}$$

ii)

$$N = \frac{g}{2\pi} = \frac{\omega \cdot t}{2\pi} \quad (3)$$

$I_{cm} = 0,24$

$$\Sigma F_x = 0 \Rightarrow v = 6 \text{ rad/s}$$

$$\Sigma \tau = 0 \Rightarrow \omega = 6 \text{ rad/s}$$

$$S = v_{cm} t \rightarrow \boxed{t = \frac{g}{6} \text{ s}}$$

$$\omega = \frac{v_{cm}}{r} = \frac{6}{0,1} = 60 \text{ rad/s}$$

$$(3) \quad N = \frac{60 \cdot \frac{g}{6}}{2\pi} \rightarrow \boxed{N = 5 \text{ nsp.}} \quad \leftarrow \text{Σ}$$



Αρσενικό  
Καδμ

Σ ΧΝΕΚΕΙΑ

